

Ξ baryon strong decays in a chiral quark model

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The strong decays of Ξ baryons up to $N = 2$ shell were studied in a chiral quark model. The strong decay properties of these well-established ground decuplet baryons were reasonably described. We found that (i) $\Xi(1690)$ and $\Xi(1820)$ could be assigned to the spin-parity $J^P = 1/2^-$ state $|70,^2 8, 1, 1, \frac{1}{2}^-\rangle$ and the spin-parity $J^P = 3/2^-$ state $|70,^2 8, 1, 1, \frac{3}{2}^-\rangle$, respectively. Slight configuration mixing might exist in these two negative parity states. (ii) $\Xi(1950)$ might correspond to several different Ξ resonances. The broad states ($\Gamma \sim 100$ MeV) observed in the $\Xi\pi$ channel could be classified as the pure $J^P = 5/2^-$ octet state $\Xi^0|70,^4 8, 1, 1, \frac{5}{2}^-\rangle$ or the mixed state $|\Xi\frac{1}{2}^-\rangle_3$ with $J^P = 1/2^-$. The Ξ resonances with moderate width ($\Gamma \sim 60$ MeV) observed in the $\Xi\pi$ channel might correspond to the $J^P = 1/2^+$ excitation $|56,^4 10, 2, 2, \frac{1}{2}^+\rangle$. The second orbital excitation $|56,^4 10, 2, 2, \frac{3}{2}^+\rangle$ and the mixed state $|\Xi\frac{1}{2}^-\rangle_1$ might be candidates for the narrow width state observed in the $\Lambda\bar{K}$ channel, however, their spin-parity numbers are incompatible with the moment analysis of the data. (iii) $\Xi(2030)$ could not be assigned to either any spin-parity $J^P = 7/2^+$ states or any pure $J^P = 5/2^+$ configurations. It seems to favor the $|70,^2 8, 2, 2, \frac{3}{2}^+\rangle$ assignment, however, its spin conflicts with the moment analysis of the data. To find more Ξ resonances, the observations in the $\Xi(1530)\pi$ and $\Sigma(1385)\bar{K}$ channels are necessary.

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I. INTRODUCTION

Understanding the baryon spectrum and the search for the missing baryon resonances are hot topics in hadron physics. For the scarcity of high quality anti-kaon beam and the small production rate for the Ξ resonances via an electromagnetic probe, the Ξ spectrum is still far from being established. There are only a few data on the Ξ resonances from the old bubble chamber experiments with small statistics. Among the eleven Ξ baryons listed in the review of the Particle Data Group (PDG) [1], only the ground octet and decuplet, $\Xi(1320)$ and $\Xi(1530)$, are well established with four-star ratings. Although the resonances $\Xi(1690)$, $\Xi(1820)$, $\Xi(1950)$ and $\Xi(2030)$ are three-star states in PDG, only $\Xi(1820)$ has a determined spin-parity $J^P = 3/2^-$.

A few theoretical studies of the Ξ baryon spectrum can be found in the literature [2–11]. All of the phenomenological models can well explain the two ground states $\Xi(1320)$ and $\Xi(1530)$, however, their predictions for the excitations are very different. For example, there is a lot of controversy about the spin-parity of $\Xi(1690)$. It might be the first radial excitation of Ξ with $J^P = 1/2^+$ according to the mass calculations with a nonrelativistic quark model by Chao *et al.* [2]. This classification was also supported by the recent quark model study of Melde *et al.* [10]. However, with a relativized quark model Capstick and Isgur predicted that the first radial excitation of Ξ should have a larger mass of ~ 1840 MeV [3]. Recently, Pervin and Roberts suggested that $\Xi(1690)$ could be assigned to the first orbital excitation of Ξ with $J^P = 1/2^-$, although their quark model predicted mass is about 35 MeV heavier than the mass of $\Xi(1690)$ [8]. They believed that a more microscopic treatment of spin-orbit in-

teractions, can be expected to drive this state to slightly lower mass. The calculations from the Skyrme model also indicated that $\Xi(1690)$ should have $J^P = 1/2^-$ [9]. Furthermore, $\Xi(1690)$ was discussed to be a dynamically generated state with $J^P = 1/2^-$ [12, 13]. It should be mentioned that BABAR collaboration, in a study of $\Lambda_c^+ \rightarrow \Xi^- \pi^+ K^+$, recently found some evidences that $\Xi(1690)$ has $J^P = 1/2^-$ [14].

Even for the $\Xi(1820)$ with well determined spin-parity quantum numbers, $J^P = 3/2^-$, there still exist many puzzles in the explanations of its nature. Considering $\Xi(1820)$ as a $J^P = 3/2^-$ orbital excitation, its mass and decay properties could be well explained in the nonrelativistic quark model [2] and algebraic model [5]. However, considering $\Xi(1820)$ as a $J^P = 3/2^-$ excitation, the mass of $\Xi(1820)$ is obviously underestimated by the relativized quark model [3] and one-boson exchange model [4]. In the unitary chiral approaches, $\Xi(1820)$ was even suggested to be a dynamically generated state from the Δ decuplet-pion octet chiral interaction [12, 13].

Although $\Xi(1950)$ is a three-star state listed in PDG, not much can be said about its properties [1]. According to various phenomenological model predictions [2, 15, 16], many states with spin-parity quantum numbers, $J^P = 1/2^\pm$, $3/2^\pm$ and $5/2^\pm$, could be candidates for $\Xi(1950)$, because their predicted masses are close to 1950 MeV. Alitti *et al.* suggested that the broad Ξ resonance ($\Gamma = 80 \pm 40$ MeV) with a mass of $M = 1930 \pm 20$ MeV observed by them could be classified as the pure $J^P = 5/2^-$ octet state [17]. With this assignment, the mass and total and partial decay widths seemed to be reasonably understood. However, the observations of Biagi *et al.* [18] do not satisfy this classification. Although they observed a Ξ resonance around 1950 MeV in the $\Lambda\bar{K}$ invariant mass distribution, its favorable spin-parity should be $5/2^+$ or its spin should be greater than $5/2$ in the natural spin-parity series $7/2^-, 9/2^+$, etc [18]. In fact, there might be more than one Ξ near 1950 MeV [1]. Recently, Valderrama, Xie and Nieves proposed the existence of three $\Xi(1950)$ states: one of

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these states would be part of a spin-parity $1/2^+$ decuplet and the other two probably would belong to the $5/2^+$ and $5/2^-$ octets [19].

About $\Xi(2030)$, not many discussions can be found in the literature. A moment analysis of [20] suggested that the spin of $\Xi(2030)$ should be $J \geq 5/2$. According to the SU(3) symmetry of hadrons, Samios *et al.* predicted that $\Xi(2030)$ was most likely to be the partner of $N(1680)$, $\Lambda(1820)$ and $\Sigma(1915)$ with $J^P = 5/2^+$ [21]. The quark model mass calculations indicated that the second $J^P = 5/2^+$ state and $J^P = 7/2^+$ state might be candidates for $\Xi(2030)$ [2, 8]. However, the recent strong decay analysis of [19] did not support the classification of [21].

Fortunately, the situation of the poor knowledge about these hyperon resonances is to be changed completely with the running of the Japan Proton Accelerator Research Complex (J-PARC) facility, where high quality anti-kaon beam will be available very soon [22]. Then, the Ξ baryons can be directly produced on the nucleons by the process $\bar{K}N \rightarrow \Xi K$ with large production cross sections. Furthermore, the investigation of Ξ baryons is also one of the major parts of the physics programs at PANDA via the process $\bar{p}p \rightarrow \Xi\bar{\Xi}$ [23], at Jlab via the photo-production processes, $\gamma p \rightarrow K^+ K^+ \Xi^-$ and $\gamma p \rightarrow K^+ K^+ \Xi^0 \pi^-$ [24–26], and at BESIII via the process Charmonium $\rightarrow \Xi\bar{\Xi}$ [27, 28], etc. Thus, these new facilities provide us good chances to study the Ξ spectrum.

Stimulated by the great progresses achieved in experiments, more and more theoretical interests begin to focus on the Ξ physics. For example, some theoretical studies of the production of Ξ via $\bar{K}N \rightarrow \Xi K$ [29, 30] and $\gamma p \rightarrow K^+ K^+ \Xi^-$ [31, 32], and the determination of the parity of Ξ resonances in these reactions were started recently [33]. In this work, we make a systematic study of the strong decays of the Ξ resonances in a chiral quark model, which has been developed and successfully used to deal with the strong decays of charmed baryons and heavy-light mesons [34–37]. Here, we mainly focus on the three-star Ξ resonances $\Xi(1690)$, $\Xi(1820)$, $\Xi(1950)$ and $\Xi(2030)$.

This work is organized as follows. In the subsequent section, baryons in the constituent quark model is outlined. Then a brief review of the strong decays described within a chiral quark model approach is given in Sec. III. The numerical results are presented and discussed in Sec. IV. Finally, a summary is given in Sec. V.

II. BARYONS IN THE QUARK MODEL

A. Spatial wave-functions

A baryon containing three quarks may be described by an oscillator potential Hamilton [38] in a nonrelativistic form:

$$\mathcal{H} = \sum_{i=1}^3 \frac{p_i^2}{2m_i} + \frac{1}{2}K \sum_{i<j} (\mathbf{r}_j - \mathbf{r}_i)^2, \quad (1)$$

where the \mathbf{r}_i and \mathbf{p}_i are the coordinate and momentum for the i -th quark in the baryon rest frame. The quarks are confined

in an oscillator potential with the potential parameter K independent of the flavor quantum number. One defines the Jacobi coordinates to eliminate the center mass (c.m.) variables:

$$\vec{\rho} = \frac{1}{\sqrt{2}}(\mathbf{r}_1 - \mathbf{r}_2), \quad (2)$$

$$\vec{\lambda} = \frac{1}{\sqrt{6}} \left(\frac{m_1 \mathbf{r}_1 + m_2 \mathbf{r}_2}{m_1 + m_2} - 2\mathbf{r}_3 \right), \quad (3)$$

$$\mathbf{R}_{c.m.} = \frac{m_1 \mathbf{r}_1 + m_2 \mathbf{r}_2 + m_3 \mathbf{r}_3}{M}, \quad (4)$$

where $M \equiv m_1 + m_2 + m_3$. Using the Jacobi coordinates in Eqs. (2)-(4), the oscillator Hamiltonian (1) is reduced to

$$\mathcal{H} = \frac{p_{c.m.}^2}{2M} + \frac{1}{2m_\rho} \mathbf{p}_\rho^2 + \frac{1}{2m_\lambda} \mathbf{p}_\lambda^2 + \frac{3}{2}K(\rho^2 + \lambda^2), \quad (5)$$

where

$$\mathbf{p}_\rho = m_\rho \dot{\vec{\rho}}, \quad \mathbf{p}_\lambda = m_\lambda \dot{\vec{\lambda}}, \quad \mathbf{P}_{c.m.} = M \dot{\mathbf{R}}_{c.m.}, \quad (6)$$

with

$$m_\lambda = \frac{3(m_1 + m_2)m_3}{2M}, \quad m_\rho = \frac{2m_1 m_2}{m_1 + m_2}. \quad (7)$$

For a Ξ baryon, it contains two strange (s) quarks and a light u/d quark. According to Eqs.(2)-(4), the coordinates, \mathbf{r}_1 , \mathbf{r}_2 and \mathbf{r}_3 , can be translated into functions of the Jacobi coordinates λ and ρ , which are given by

$$\mathbf{r}_1 = \mathbf{R}_{c.m.} + \frac{1}{\sqrt{6}} \frac{3m'}{2m + m'} \vec{\lambda} + \frac{1}{\sqrt{2}} \vec{\rho}, \quad (8)$$

$$\mathbf{r}_2 = \mathbf{R}_{c.m.} + \frac{1}{\sqrt{6}} \frac{3m'}{2m + m'} \vec{\lambda} - \frac{1}{\sqrt{2}} \vec{\rho}, \quad (9)$$

$$\mathbf{r}_3 = \mathbf{R}_{c.m.} - \sqrt{\frac{2}{3}} \frac{3m}{2m + m'} \vec{\lambda}. \quad (10)$$

Then, the momenta \mathbf{p}_1 , \mathbf{p}_2 and \mathbf{p}_3 are given by

$$\mathbf{p}_1 = \frac{m}{M} \mathbf{P}_{c.m.} + \frac{1}{\sqrt{6}} \mathbf{p}_\lambda + \frac{1}{\sqrt{2}} \mathbf{p}_\rho, \quad (11)$$

$$\mathbf{p}_2 = \frac{m}{M} \mathbf{P}_{c.m.} + \frac{1}{\sqrt{6}} \mathbf{p}_\lambda - \frac{1}{\sqrt{2}} \mathbf{p}_\rho, \quad (12)$$

$$\mathbf{p}_3 = \frac{m'}{M} \mathbf{P}_{c.m.} - \sqrt{\frac{2}{3}} \mathbf{p}_\lambda, \quad (13)$$

where m and m' stand for the masses of strange and u/d quarks, respectively.

The spatial wave-function is a product of the ρ -oscillator and the λ -oscillator states. With the standard notation, the principal quantum numbers of the ρ -oscillator and λ -oscillator are $N_\rho = (2n_\rho + l_\rho)$ and $N_\lambda = (2n_\lambda + l_\lambda)$, and the energy of a state is given by

$$E_N = \left(N_\rho + \frac{3}{2} \right) \omega_\rho + \left(N_\lambda + \frac{3}{2} \right) \omega_\lambda. \quad (14)$$

The total principal quantum number (i.e. shell number) N is defined as

$$N = N_\rho + N_\lambda, \quad (15)$$

and the frequencies of the ρ -mode and λ -mode are

$$\omega_\lambda = (3K/m_\lambda)^{1/2}, \quad \omega_\rho = (3K/m_\rho)^{1/2}. \quad (16)$$

In the constituent quark model, a useful oscillator parameter, i.e. the potential strength is defined as

$$\alpha_\lambda = (m_\lambda \omega_\lambda)^{1/2} = \left(\frac{3m'}{2m + m'} \right)^{1/4} \alpha_\rho. \quad (17)$$

For a Ξ baryon, the constituent mass of a strange quark is close to that of a u/d quark. Thus, the relation

$$\alpha_\lambda \simeq \alpha_\rho \equiv \alpha_h, \quad (18)$$

is a good approximation.

The total spatial wave-function of the oscillator Hamiltonian can be written as [39, 40]

$$\Psi(\mathbf{r}_1, \mathbf{r}_2, \mathbf{r}_3) = \frac{e^{i\mathbf{P}_{c.m.} \cdot \mathbf{R}_{c.m.}}}{\sqrt{(2\pi)^3}} \Psi_{NLL_z}^\sigma(\vec{\rho}, \vec{\lambda}), \quad (19)$$

where $\Psi_{NLL_z}^\sigma(\vec{\rho}, \vec{\lambda})$ is the harmonic oscillator wavefunction, and the $\sigma = s, \rho, \lambda, a$ stands for the representation of the S_3 group. The harmonic oscillator wavefunction is given by [39, 40]

$$\Psi_{NLL_z}^\sigma(\vec{\rho}, \vec{\lambda}) = P_{NLL_z}^\sigma \frac{\alpha_h^3}{\pi^{3/2}} e^{-\alpha_h^2(\vec{\rho}^2 + \vec{\lambda}^2)/2}, \quad (20)$$

where $P_{NLL_z}^\sigma$ is a polynomial of ρ and λ . Explicitly, the states within $N \leq 2$ can be obtained [40]:

$$N = 0, \quad L = 0, \quad P_{000}^s = 1, \quad (21)$$

$$N = 1, \quad L = 1, \quad P_{111}^\rho = \alpha_h \rho_+, \quad (22)$$

$$P_{111}^\lambda = \alpha_h \lambda_+, \quad (23)$$

$$N = 2, \quad L = 0, \quad P_{200}^s = \frac{\alpha_h^2}{\sqrt{3}}(\vec{\rho}^2 + \vec{\lambda}^2 - 3\alpha_h^{-2}), \quad (24)$$

$$P_{200}^\rho = \frac{\alpha_h^2}{\sqrt{3}} 2\vec{\rho} \cdot \vec{\lambda}, \quad (25)$$

$$P_{200}^\lambda = \frac{\alpha_h^2}{\sqrt{3}}(\vec{\rho}^2 - \vec{\lambda}^2), \quad (26)$$

$$L = 2, \quad P_{222}^s = \frac{1}{2}\alpha_h^2(\rho_+^2 + \lambda_+^2), \quad (27)$$

$$P_{222}^\rho = \alpha_h^2 \rho_+ \lambda_+, \quad (28)$$

$$P_{222}^\lambda = \frac{1}{2}\alpha_h^2(\rho_+^2 - \lambda_+^2), \quad (29)$$

$$L = 1, \quad P_{211}^a = \alpha_h^2(\rho_+ \lambda_z - \lambda_+ \rho_z). \quad (30)$$

B. Flavor and spin wave-functions

In the quark model, the SU(3) flavor wave-functions of the symmetry decuplet are [40]

$$\phi^s = \begin{cases} uuu, & \Delta^{++} \\ \frac{1}{\sqrt{3}}(uud + udu + duu), & \Delta^+ \\ \frac{1}{\sqrt{3}}(uus + usu + suu), & \Sigma^{*+} \\ ddd, & \Delta^- \\ \frac{1}{\sqrt{3}}(udd + dud + ddu), & \Delta^0 \\ \frac{1}{\sqrt{3}}(dds + dsd + sdd), & \Sigma^{*-} \\ sss, & \Omega \\ \frac{1}{\sqrt{3}}(uss + sus + ssu), & \Xi^{*0} \\ \frac{1}{\sqrt{3}}(dss + sds + ssd), & \Xi^{*-} \\ \frac{1}{\sqrt{6}}(uds + sud + dsu + sdu + dus + usd), & \Sigma^{*0} \end{cases} \quad (31)$$

the mixed-symmetry octet wave-functions are [40]

$$\phi^\lambda = \begin{cases} \frac{1}{\sqrt{6}}(2uud - duu - udu), & p \\ \frac{1}{\sqrt{6}}(dud + udd - 2ddu), & n \\ \frac{1}{\sqrt{6}}(2uus - suu - usu), & \Sigma^+ \\ \frac{1}{2\sqrt{3}}(sdu + sud + usd + dsu - 2uds - 2dus), & \Sigma^0 \\ \frac{1}{\sqrt{6}}(2dds - sdd - dsd), & \Sigma^- \\ \frac{1}{2}(sud + usd - sdu - dsu), & \Lambda \\ \frac{1}{\sqrt{6}}(sus + uss - 2ssu), & \Xi^0 \\ \frac{1}{\sqrt{6}}(dss + sds - 2ssd), & \Xi^- \end{cases} \quad (32)$$

while the mixed-antisymmetric octet wave-functions are [40]

$$\phi^\rho = \begin{cases} \frac{1}{\sqrt{2}}(udu - duu), & p \\ \frac{1}{\sqrt{2}}(udd - dud), & n \\ \frac{1}{\sqrt{2}}(usu - suu), & \Sigma^+ \\ \frac{1}{2}(sud + sdu - usd - dsu), & \Sigma^0 \\ \frac{1}{\sqrt{2}}(dsd - sdd), & \Sigma^- \\ \frac{1}{2\sqrt{3}}(usd + sdu - sud - dsu - 2dus + 2uds), & \Lambda \\ \frac{1}{\sqrt{2}}(uss - sus), & \Xi^0 \\ \frac{1}{\sqrt{2}}(dss - sds), & \Xi^- \end{cases} \quad (33)$$

The total antisymmetric singlet flavor wave-function is

$$\phi^a = \frac{1}{\sqrt{6}}(uds + dsu + sud - dus - usd - sdu). \quad (34)$$

In the quark model, the typical SU(2) spin wave-functions for the baryons can be adopted [41, 42]:

$$\begin{aligned} \chi_{3/2}^s &= \uparrow\uparrow\uparrow, \quad \chi_{-3/2}^s = \downarrow\downarrow\downarrow, \\ \chi_{1/2}^s &= \frac{1}{\sqrt{3}}(\uparrow\uparrow\downarrow + \uparrow\downarrow\uparrow + \downarrow\uparrow\uparrow), \\ \chi_{-1/2}^s &= \frac{1}{\sqrt{3}}(\uparrow\downarrow\downarrow + \downarrow\downarrow\uparrow + \downarrow\uparrow\downarrow), \end{aligned} \quad (35)$$

for the spin-3/2 states with symmetric spin wave-functions,

$$\begin{aligned}\chi_{1/2}^\rho &= \frac{1}{\sqrt{2}}(\uparrow\uparrow\uparrow - \downarrow\uparrow\uparrow), \\ \chi_{-1/2}^\rho &= \frac{1}{\sqrt{2}}(\uparrow\downarrow\downarrow - \downarrow\uparrow\downarrow),\end{aligned}\quad (36)$$

for the spin-1/2 states with mixed antisymmetric spin wave-functions, and

$$\begin{aligned}\chi_{1/2}^\lambda &= -\frac{1}{\sqrt{6}}(\uparrow\uparrow\uparrow + \downarrow\uparrow\uparrow - 2\uparrow\uparrow\downarrow), \\ \chi_{-1/2}^\lambda &= +\frac{1}{\sqrt{6}}(\uparrow\downarrow\downarrow + \downarrow\uparrow\downarrow - 2\downarrow\downarrow\uparrow),\end{aligned}\quad (37)$$

for the spin-1/2 states with mixed symmetric spin wave-functions.

The flavor-spin wave-functions are representations of SU(6), which are denoted by $|N_6, {}^{2S+1}N_3\rangle$, where N_6 (N_3) represents the SU(6) (SU(3)) representation and S stands for the total spin of the wave-function. The symmetric **56** representation wave-functions are [40]

$$|56, {}^2 8\rangle^s = \frac{1}{\sqrt{2}}(\phi^\rho \chi^\rho + \phi^\lambda \chi^\lambda), \quad (38)$$

$$|56, {}^4 10\rangle^s = \phi^s \chi^s, \quad (39)$$

the antisymmetric **70** representation wave-functions are [40]

$$|70, {}^2 8\rangle^\rho = \frac{1}{\sqrt{2}}(\phi^\rho \chi^\lambda + \phi^\lambda \chi^\rho), \quad (40)$$

$$|70, {}^4 8\rangle^\rho = \phi^\rho \chi^s, \quad (41)$$

$$|70, {}^2 10\rangle^\rho = \phi^s \chi^\rho, \quad (42)$$

$$|70, {}^2 1\rangle^\rho = \phi^\alpha \chi^\lambda, \quad (43)$$

while the symmetric **70** representation wave-functions are [40]

$$|70, {}^2 8\rangle^\lambda = \frac{1}{\sqrt{2}}(\phi^\rho \chi^\rho - \phi^\lambda \chi^\lambda), \quad (44)$$

$$|70, {}^4 8\rangle^\lambda = \phi^\lambda \chi^s, \quad (45)$$

$$|70, {}^2 10\rangle^\lambda = \phi^s \chi^\lambda, \quad (46)$$

$$|70, {}^2 1\rangle^\lambda = \phi^\alpha \chi^\rho, \quad (47)$$

and the antisymmetric **20** representation wave-functions are [40]

$$|20, {}^2 8\rangle^a = \frac{1}{\sqrt{2}}(\phi^\rho \chi^\lambda - \phi^\lambda \chi^\rho), \quad (48)$$

$$|20, {}^4 1\rangle^a = \phi^a \chi^s. \quad (49)$$

C. Total wave-functions

The total spin-flavor-space wave-functions are the SU(6) \otimes O(3) representations, which are denoted by

$$|SU(6) \otimes O(3)\rangle = |N_6, {}^{2S+1}N_3, N, L, J^P\rangle. \quad (50)$$

The spin-flavor-space wave-functions have to be permutation-symmetric because the baryon color wave-function is totally anti-symmetric. The spin-flavor-space wave-functions up to $N = 2$ shell are listed in Tab. I. So far no experimental evidence for the existence of the **20** SU(6) representation has been found, thus, we do not consider these excitations in this work.

TABLE I: The spin-flavor-space wave-functions of different light baryons, denoted by $|N_6, {}^{2S+1}N_3, N, L, J^P\rangle$. The Clebsch-Gordan series for the spin and angular-momentum addition $|J, J_z\rangle = \sum_{L_z+S_z=J_z} \langle LL_z, SS_z | JJ_z \rangle \Psi_{NLL_z}^\sigma \chi_{S_z}$ has been omitted.

state	N	J	L	S	wave-function
$ 56, {}^2 8, 0, 0, \frac{1}{2}^+\rangle$	0	$\frac{1}{2}$	0	$\frac{1}{2}$	$ 56, {}^2 8\rangle \Psi_{000}^s$
$ 56, {}^4 10, 0, 0, \frac{3}{2}^+\rangle$	0	$\frac{3}{2}$	0	$\frac{3}{2}$	$ 56, {}^4 10\rangle \Psi_{000}^s$
$ 56, {}^2 8, 2, 0, \frac{1}{2}^+\rangle$	2	$\frac{1}{2}$	0	$\frac{1}{2}$	$ 56, {}^2 8\rangle \Psi_{200}^s$
$ 56, {}^4 10, 2, 0, \frac{3}{2}^+\rangle$	2	$\frac{3}{2}$	0	$\frac{3}{2}$	$ 56, {}^4 10\rangle \Psi_{200}^s$
$ 56, {}^2 8, 2, 2, \frac{3}{2}^+\rangle$	2	$\frac{5}{2}$	2	$\frac{1}{2}$	$ 56, {}^2 8\rangle \Psi_{22L_z}^s$
$ 56, {}^2 8, 2, 2, \frac{5}{2}^+\rangle$	2	$\frac{5}{2}$	2	$\frac{1}{2}$	
$ 56, {}^4 10, 2, 2, \frac{1}{2}^+\rangle$	2	$\frac{7}{2}$	2	$\frac{3}{2}$	$ 56, {}^4 10\rangle \Psi_{22L_z}^s$
$ 56, {}^4 10, 2, 2, \frac{3}{2}^+\rangle$	2	$\frac{7}{2}$	2	$\frac{3}{2}$	
$ 56, {}^4 10, 2, 2, \frac{5}{2}^+\rangle$	2	$\frac{7}{2}$	2	$\frac{3}{2}$	
$ 56, {}^4 10, 2, 2, \frac{7}{2}^+\rangle$	2	$\frac{7}{2}$	2	$\frac{3}{2}$	
$ 70, {}^2 8, 1, 1, \frac{1}{2}^-\rangle$	1	$\frac{3}{2}$	1	$\frac{1}{2}$	$ 70, {}^2 8\rangle^\rho \Psi_{11L_z}^\rho + 70, {}^2 8\rangle^\lambda \Psi_{11L_z}^\lambda$
$ 70, {}^2 8, 1, 1, \frac{3}{2}^-\rangle$	1	$\frac{3}{2}$	1	$\frac{1}{2}$	
$ 70, {}^4 8, 1, 1, \frac{1}{2}^-\rangle$	1	$\frac{5}{2}$	1	$\frac{3}{2}$	$ 70, {}^4 8\rangle^\rho \Psi_{11L_z}^\rho + 70, {}^4 8\rangle^\lambda \Psi_{11L_z}^\lambda$
$ 70, {}^4 8, 1, 1, \frac{3}{2}^-\rangle$	1	$\frac{5}{2}$	1	$\frac{3}{2}$	
$ 70, {}^4 8, 1, 1, \frac{5}{2}^-\rangle$	1	$\frac{5}{2}$	1	$\frac{3}{2}$	
$ 70, {}^4 8, 1, 1, \frac{7}{2}^-\rangle$	1	$\frac{5}{2}$	1	$\frac{3}{2}$	
$ 70, {}^2 10, 1, 1, \frac{1}{2}^-\rangle$	1	$\frac{3}{2}$	1	$\frac{1}{2}$	$ 70, {}^2 10\rangle^\rho \Psi_{11L_z}^\rho + 70, {}^2 10\rangle^\lambda \Psi_{11L_z}^\lambda$
$ 70, {}^2 10, 1, 1, \frac{3}{2}^-\rangle$	1	$\frac{3}{2}$	1	$\frac{1}{2}$	
$ 70, {}^2 8, 2, 0, \frac{1}{2}^+\rangle$	2	$\frac{1}{2}$	0	$\frac{1}{2}$	$ 70, {}^2 8\rangle^\rho \Psi_{200}^\rho + 70, {}^2 8\rangle^\lambda \Psi_{200}^\lambda$
$ 70, {}^4 8, 2, 0, \frac{3}{2}^+\rangle$	2	$\frac{3}{2}$	0	$\frac{3}{2}$	$ 70, {}^4 8\rangle^\rho \Psi_{200}^\rho + 70, {}^4 8\rangle^\lambda \Psi_{200}^\lambda$
$ 70, {}^2 10, 2, 0, \frac{1}{2}^+\rangle$	2	$\frac{1}{2}$	0	$\frac{1}{2}$	$ 70, {}^2 10\rangle^\rho \Psi_{200}^\rho + 70, {}^2 10\rangle^\lambda \Psi_{200}^\lambda$
$ 70, {}^2 8, 2, 2, \frac{3}{2}^+\rangle$	2	$\frac{5}{2}$	2	$\frac{1}{2}$	$ 70, {}^2 8\rangle^\rho \Psi_{22L_z}^\rho + 70, {}^2 8\rangle^\lambda \Psi_{22L_z}^\lambda$
$ 70, {}^2 8, 2, 2, \frac{5}{2}^+\rangle$	2	$\frac{5}{2}$	2	$\frac{1}{2}$	
$ 70, {}^4 8, 2, 2, \frac{1}{2}^+\rangle$	2	$\frac{7}{2}$	2	$\frac{3}{2}$	$ 70, {}^4 8\rangle^\rho \Psi_{22L_z}^\rho + 70, {}^4 8\rangle^\lambda \Psi_{22L_z}^\lambda$
$ 70, {}^4 8, 2, 2, \frac{3}{2}^+\rangle$	2	$\frac{7}{2}$	2	$\frac{3}{2}$	
$ 70, {}^4 8, 2, 2, \frac{5}{2}^+\rangle$	2	$\frac{7}{2}$	2	$\frac{3}{2}$	
$ 70, {}^4 8, 2, 2, \frac{7}{2}^+\rangle$	2	$\frac{7}{2}$	2	$\frac{3}{2}$	
$ 70, {}^2 10, 2, 2, \frac{3}{2}^+\rangle$	2	$\frac{5}{2}$	2	$\frac{1}{2}$	$ 70, {}^2 10\rangle^\rho \Psi_{22L_z}^\rho + 70, {}^2 10\rangle^\lambda \Psi_{22L_z}^\lambda$
$ 70, {}^2 10, 2, 2, \frac{5}{2}^+\rangle$	2	$\frac{5}{2}$	2	$\frac{1}{2}$	

III. STRONG DECAY OF A BARYON IN THE CHIRAL QUARK MODEL

In the chiral quark model, the effective low energy quark-meson pseudoscalar coupling at tree level is given by [43–46]

$$H_m = \sum_j \frac{1}{f_m} \bar{\psi}_j \gamma_\mu^j \gamma_5^j \psi_j \vec{\tau} \cdot \partial^\mu \vec{\phi}_m, \quad (51)$$

where ψ_j represents the j -th quark field in a baryon, and f_m is the meson's decay constant. The pseudoscalar meson octet

ϕ_m is expressed as

$$\phi_m = \begin{pmatrix} \frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta & \pi^+ & K^+ \\ \pi^- & -\frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta & K^0 \\ K^- & \bar{K}^0 & -\sqrt{\frac{2}{3}}\eta \end{pmatrix}. \quad (52)$$

To match the nonrelativistic harmonic oscillator spatial wave function ${}^N\Psi_{LL_z}$ in the quark model, we adopt the nonrelativistic form of Eq. (51) in the calculations, which is given by [43–46]

$$H_m^{nr} \simeq \sum_{j=1}^3 \left\{ \frac{\omega_m}{E_f + M_f} \boldsymbol{\sigma}_j \cdot \mathbf{P}_f + \frac{\omega_m}{E_i + M_i} \boldsymbol{\sigma}_j \cdot \mathbf{P}_i - \boldsymbol{\sigma}_j \cdot \mathbf{q} + \frac{\omega_m}{2\mu_q} \boldsymbol{\sigma}_j \cdot \mathbf{p}'_j \right\} I_j \varphi_m, \quad (53)$$

where $\boldsymbol{\sigma}_j$ is the Pauli spin operator on the j -th quark of the baryon, and μ_q is a reduced mass given by $1/\mu_q = 1/m_j + 1/m'_j$ with m_j and m'_j for the masses of the j -th quark in the initial and final baryons, respectively. For emitting a meson, we have $\varphi_m = e^{-i\mathbf{q}\cdot\mathbf{r}_j}$, and for absorbing a meson we have $\varphi_m = e^{i\mathbf{q}\cdot\mathbf{r}_j}$. In the above nonrelativistic expansion, $\mathbf{p}'_j (= \mathbf{p}_j - m_j/M\mathbf{P}_{c.m.})$ is the internal momentum operator for the j -th quark in the baryon rest frame. ω_m and \mathbf{q} are the energy and three-vector momentum of the meson, respectively. \mathbf{P}_i and \mathbf{P}_f stand for the momenta of the initial final baryons, respectively. The isospin operator I_j in Eq. (53) is expressed as

$$I_j = \begin{cases} a_j^\dagger(u)a_j(s) & \text{for } K^+, \\ a_j^\dagger(s)a_j(u) & \text{for } K^-, \\ a_j^\dagger(d)a_j(s) & \text{for } K^0, \\ a_j^\dagger(s)a_j(d) & \text{for } \bar{K}^0, \\ a_j^\dagger(u)a_j(d) & \text{for } \pi^-, \\ a_j^\dagger(d)a_j(u) & \text{for } \pi^+, \\ \frac{1}{\sqrt{2}}[a_j^\dagger(u)a_j(u) - a_j^\dagger(d)a_j(d)] & \text{for } \pi^0, \\ \frac{1}{\sqrt{2}}[a_j^\dagger(u)a_j(u) + a_j^\dagger(d)a_j(d)] \cos \phi_p & \\ -a_j^\dagger(s)a_j(s) \sin \phi_p & \text{for } \eta, \end{cases} \quad (54)$$

where $a_j^\dagger(u, d, s)$ and $a_j(u, d, s)$ are the creation and annihilation operators for the u , d and s quarks, and ϕ_p is the mixing angle of η meson in the flavor basis [1, 47].

In the calculations, we select the initial-baryon-rest system for the decay precesses. The energies and momenta of the initial baryons are denoted by (E_i, \mathbf{P}_i) , while those of the final state mesons and baryons are denoted by (ω_f, \mathbf{q}) and (E_f, \mathbf{P}_f) , respectively. Note that $\mathbf{P}_i = 0$ and $\mathbf{P}_f = -\mathbf{q}$. For a light pseudoscalar meson emission in the strong decay process of a baryon, $\mathcal{B} \rightarrow \mathcal{B}'\mathbb{M}(\mathbf{q})$, the partial decay amplitudes can be worked out according to

$$\mathcal{M}[\mathcal{B} \rightarrow \mathcal{B}'\mathbb{M}(\mathbf{q})] = 3 \left\langle \mathcal{B}' \left| \left[G\boldsymbol{\sigma}_3 \cdot \mathbf{q} + h\boldsymbol{\sigma}_3 \cdot \mathbf{p}'_3 \right] I_3 e^{-i\mathbf{q}\cdot\mathbf{r}_3} \right| \mathcal{B} \right\rangle \quad (55)$$

with

$$G \equiv -\frac{\omega_m}{E_f + M_f} - 1, \quad h \equiv \frac{\omega_m}{2\mu_q}, \quad (56)$$

where \mathcal{B} and \mathcal{B}' stand for the initial and final baryon wave-functions listed in Tab. I.

With the derived decay amplitudes, one can calculate the width by [34]

$$\Gamma = \left(\frac{\delta}{f_m} \right)^2 \frac{(E_f + M_f)|q|}{4\pi M_i} \frac{1}{2J_i + 1} \sum_{J_{iz}, J_{fz}} |\mathcal{M}_{J_{iz}, J_{fz}}|, \quad (57)$$

where the J_{iz} and J_{fz} stand for the the total angular momenta of the initial and final baryons, respectively. δ as a global parameter accounts for the strength of the quark-meson couplings.

In the calculation, the standard quark model parameters are adopted. Namely, we set $m_u = m_d = 350$ MeV, $m_s = 450$ MeV, for the constituent quark masses. The harmonic oscillator parameter α_h in the wave-function ${}^N\Psi_{LL_z}$ is taken as $\alpha_h = 0.40$ GeV. The decay constants for π , K and η mesons are taken as $f_\pi = 132$ MeV, $f_K = f_\eta = 160$ MeV, respectively. The masses of the mesons and baryons used in the calculations are adopted from the Particle Data Group [1].

IV. RESULTS AND ANALYSIS

TABLE II: The partial and total decay widths (MeV) of the well-established baryons $\Xi(1530)$, $\Sigma(1385)$ and $\Delta(1232)$, which correspond to the same representation $[56, 4, 10, 0, 0, \frac{3}{2}^+]$. The experimental data are obtained from PDG.

state	channel	Γ_i^{th}	Γ_{total}^{th}	Γ_{total}^{exp}
$\Xi(1530)^0$	$\Xi^- \pi^+$	5.6	9.1(input)	9.1 ± 0.5
	$\Xi^0 \pi^0$	3.5		
$\Xi(1530)^-$	$\Xi^0 \pi^-$	7.1	10.3	$9.9^{+1.7}_{-1.9}$
	$\Xi^- \pi^0$	3.2		
$\Sigma(1385)^+$	$\Sigma^+ \pi^0$	1.9	27.1	36 ± 0.7
	$\Sigma^0 \pi^+$	1.5		
	$\Lambda^0 \pi^+$	23.7		
$\Sigma(1385)^0$	$\Sigma^+ \pi^-$	1.8	27.9	36 ± 5
	$\Sigma^- \pi^+$	1.3		
	$\Lambda^0 \pi^0$	24.8		
$\Sigma(1385)^-$	$\Sigma^- \pi^0$	1.7	28.7	39.4 ± 2.1
	$\Sigma^0 \pi^-$	1.8		
	$\Lambda^0 \pi^-$	25.2		
$\Delta(1232)^{++}$	$p\pi^+$	63.9	63.9	$114 \sim 120$
$\Delta(1232)^+$	$p\pi^0$	43.7	64.7	$114 \sim 120$
	$n\pi^+$	21.0		
$\Delta(1232)^0$	$p\pi^-$	21.3	64.3	$114 \sim 120$
	$n\pi^0$	43.0		

A. $\Xi(1530)$

$\Xi(1530)$ is the only Ξ resonance whose properties are all reasonably well known. According to the classification of the

quark model, it is assigned to the $[56, {}^4 10, 0, 0, \frac{3}{2}^+]$ representation. In present work, the measured width for $\Xi(1530)^0 \rightarrow \Xi\pi$ as an input (i.e. $\Gamma = 9.1$ MeV [1]) to determine parameter δ in Eq.(57), which gives

$$\delta = 0.576. \quad (58)$$

With this determined parameter, we can predict the other Ξ resonance strong decays. First, the strong decays of $\Xi(1530)^-$ were calculated. The results were listed in Tab. II, where we found that our predictions are in agreement with the data. Furthermore, we have noted that $\Sigma(1385)$ and $\Delta(1232)$ also correspond to the $[56, {}^4 10, 0, 0, \frac{3}{2}^+]$ representation. They are the SU(3)-flavor counterparts of $\Xi(1530)$. Applying the determined value for δ , we calculated the strong decays of the $\Sigma(1385)$ and $\Delta(1232)$ resonances, the results were listed in Tab. II as well. It is seen that the predicted widths for $\Sigma(1385)$ are compatible with the experimental data, and the partial decay width ratio

$$\frac{\Gamma[\Sigma(1385) \rightarrow \Sigma\pi]}{\Gamma[\Sigma(1385) \rightarrow \Lambda\pi]} \simeq 0.134 \pm 0.09, \quad (59)$$

are in good agreement with the PDG value [1]. The predicted widths for $\Delta(1232)$ are roughly comparable with the data. These decay widths are underestimated with the value of $\delta = 0.576$ determined by fitting the width for $\Xi(1530)^0 \rightarrow \Xi\pi$. The value of δ is slightly smaller than that used for the study of the baryons only containing light u and/or d quarks [48].

As a whole, the predicted strong decay properties for $\Xi(1530)^-$, $\Sigma(1385)$ and $\Delta(1232)$ are compatible with the experimental data within the quark model uncertainties, which indicates that the SU(3)-flavor symmetry approximately holds in these ground decuplet baryons.

B. $\Xi(1690)$

$\Xi(1690)$ is a three-star state listed in PDG. Its decay width might be less than 30 MeV [1]. Three decay modes $\Lambda\bar{K}$, $\Sigma\bar{K}$ and $\Xi\pi$ were observed in experiments. Recently, *BABAR* Collaboration found some evidences that the $\Xi(1690)$ has $J^P = 1/2^-$ in the study of $\Lambda_c^+ \rightarrow \Xi^-\pi^+K^+$ [14].

If $\Xi(1690)$ is a $J^P = 1/2^-$ resonance, it should correspond to one of the first orbital excitation states: $|70, {}^2 8, 1, 1, \frac{1}{2}^- \rangle$, $|70, {}^4 8, 1, 1, \frac{1}{2}^- \rangle$ and $|70, {}^2 10, 1, 1, \frac{1}{2}^- \rangle$ or a mixed state between them.

Considering $\Xi(1690)$ as the $|70, {}^2 8, 1, 1, \frac{1}{2}^- \rangle$, $|70, {}^4 8, 1, 1, \frac{1}{2}^- \rangle$ and $|70, {}^2 10, 1, 1, \frac{1}{2}^- \rangle$, respectively, we calculated their decay properties, which were listed in Tab. III. Comparing the predictions with the measurements, we found that if $\Xi(1690)$ is assigned to $|70, {}^2 8, 1, 1, \frac{1}{2}^- \rangle$, the calculated decay width

$$\Gamma \approx 48 \text{ MeV}, \quad (60)$$

and partial decay width ratios

$$\frac{\Gamma(\Xi\pi)}{\Gamma(\Sigma\bar{K})} \simeq 0.2, \quad \frac{\Gamma(\Sigma\bar{K})}{\Gamma(\Lambda\bar{K})} \approx 1.0, \quad \frac{\Gamma(\Xi(1530)\pi)}{\Gamma(\Sigma\bar{K})} \approx 0.0002, \quad (61)$$

are roughly in agreement with the measurements. Neither $|70, {}^4 8, 1, 1, \frac{1}{2}^- \rangle$ nor $|70, {}^2 10, 1, 1, \frac{1}{2}^- \rangle$ could be considered as an assignment to $\Xi(1690)$ for their partial decay width ratios disagree with the observations.

TABLE III: The total and partial decay widths (MeV) of $\Xi(1690)$ with different $J^P = 1/2^-$ assignments.

assignment	$\Xi\pi$	$\Sigma\bar{K}$	$\Lambda\bar{K}$	$\Xi(1530)\pi$	Γ_{total}
$ 70, {}^2 8, 1, 1, \frac{1}{2}^- \rangle$	3.69	22.30	22.15	0.005	48.14
$ 70, {}^4 8, 1, 1, \frac{1}{2}^- \rangle$	59.05	5.58	22.15	0.001	86.78
$ 70, {}^2 10, 1, 1, \frac{1}{2}^- \rangle$	3.69	1.39	5.54	0.005	10.63

As we know, configuration mixing between several states with the same J^P often occurs via some interactions. Thus, $\Xi(1690)$ might be a mixed state between $|70, {}^2 8, 1, 1, \frac{1}{2}^- \rangle$, $|70, {}^4 8, 1, 1, \frac{1}{2}^- \rangle$ and $|70, {}^2 10, 1, 1, \frac{1}{2}^- \rangle$. Now, we consider the physical states with $J^P = \frac{1}{2}^-$ as mixed states between $|70, {}^2 8 \rangle$, $|70, {}^4 8 \rangle$ and $|70, {}^2 10 \rangle$. According to the standard CKM matrix method, the physical states can be express as:

$$\begin{pmatrix} |\Xi_{\frac{1}{2}^-}^1 \rangle_1 \\ |\Xi_{\frac{1}{2}^-}^1 \rangle_2 \\ |\Xi_{\frac{1}{2}^-}^1 \rangle_3 \end{pmatrix} = U \begin{pmatrix} |70, {}^2 8 \rangle \\ |70, {}^4 8 \rangle \\ |70, {}^2 10 \rangle \end{pmatrix}, \quad (62)$$

with

$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13} & c_{12}c_{23} - s_{12}s_{23}s_{13} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13} & -c_{12}s_{23} - s_{12}c_{23}s_{13} & c_{23}c_{13} \end{pmatrix}, \quad (63)$$

where $c_{ij} \equiv \cos \theta_{ij}$ and $s_{ij} \equiv \sin \theta_{ij}$ with θ_{ij} the mixing angles to be determined by the experimental data.

In present work, we take $\Xi(1690)$ as $|\Xi_{\frac{1}{2}^-}^1 \rangle_2$. By fitting the experimental data of DIONISI 78 [49] (see Tab. IV), we obtained $\theta_{12} \simeq 5^\circ$, $\theta_{13} \simeq 105^\circ$ and $\theta_{23} \simeq 95^\circ$. The theoretical predictions compared with the data were listed in Tab. IV. From the table, we found that the decay properties of $\Xi(1690)$ could be well described with these determined mixing angles. Thus, $\Xi(1690)$ could be a mixed state.

TABLE IV: The predicted total and partial decay widths (MeV) and partial decay width ratios (MeV) of $\Xi(1690) \equiv \Psi_2$ compared with the experiment data of DIONISI 78 [49]. The mixing angles are $\theta_{12} = 5^\circ$, $\theta_{13} = 75^\circ$ and $\theta_{23} = 95^\circ$.

channel	Γ_i^{th}	Γ_{total}^{th}	Γ_{total}^{exp}	channel ratio	R_{th}	R_{exp}
$\Xi\pi$	1.0	37	44_{-23}^{+23}	$\Gamma(\Sigma\bar{K})/\Gamma(\Lambda\bar{K})$	2.88	$2.7_{-0.9}^{+0.9}$
$\Sigma\bar{K}$	27.0			$\Gamma(\Xi\pi)/\Gamma(\Sigma\bar{K})$	0.04	< 0.09
$\Lambda\bar{K}$	9.4			$\Gamma(\Xi(1530)\pi)/\Gamma(\Sigma\bar{K})$	$\sim 10^{-4}$	< 0.06
$\Xi(1530)\pi$	0.01					

With these determined mixing angles, Eq.(62) can be ex-

plicitly written as

$$\begin{pmatrix} |\Xi_{\frac{1}{2}}^{-}\rangle_1 \\ |\Xi(1690)_{\frac{1}{2}}^{-}\rangle \\ |\Xi_{\frac{1}{2}}^{-}\rangle_3 \end{pmatrix} = \begin{pmatrix} -0.26 & -0.02 & 0.97 \\ -0.95 & -0.17 & -0.26 \\ 0.17 & -0.98 & 0.02 \end{pmatrix} \begin{pmatrix} |70,^2 8\rangle \\ |70,^4 8\rangle \\ |70,^2 10\rangle \end{pmatrix}, \quad (64)$$

From the above equation, it is obviously seen that the main component of the physical state $\Xi(1690)$ is $|70,^2 8, 1, 1, 1/2^{-}\rangle$ ($\sim 90\%$), which slightly mixes with $|70,^2 10, 1, 1, 1/2^{-}\rangle$ ($\sim 7\%$) and $|70,^4 8, 1, 1, 1/2^{-}\rangle$ ($\sim 3\%$).

In Ref. [50], *BABAR* Collaboration studied the spin of $\Xi(1690)$ from $\Lambda_c^+ \rightarrow \Lambda K^+ \bar{K}^0$. They found that the spin of $\Xi(1690)$ is consistent with the value $J = 1/2$. However, they could not determine the parity of $\Xi(1690)$. According to the mass predictions of quark model, the mass of the first radial ($2S$) excitation of Ξ with $J^P = \frac{1}{2}^+$ might be close to 1690 MeV [2, 10]. Thus, we should consider the possibility of $\Xi(1690)$ as the positive parity radial ($2S$) excitations with $J^P = \frac{1}{2}^+$. In the constituent quark model, there are three radial ($2S$) excitations with $J^P = \frac{1}{2}^+$: $|56,^2 8, 2, 0, \frac{1}{2}^+\rangle$, $|70,^2 8, 2, 0, \frac{1}{2}^+\rangle$ and $|70,^2 10, 2, 0, \frac{1}{2}^+\rangle$. In our calculation, those states's total decay widths are too small to compare with the experimental data. The predicted partial decay width ratios are incompatible with the observations as well. Thus, these states with $J^P = \frac{1}{2}^+$ as assignments to $\Xi(1690)$ should be excluded. Furthermore, we also studied the strong decay properties of the other first orbital excitation states with $J^P = 3/2^-$ and $J^P = 5/2^-$. Their decay properties are very different from those of $\Xi(1690)$. For simplicity, the calculated results are not shown in this work.

In a word, $\Xi(1690)$ is most likely to be the first orbital excitation of Ξ with $J^P = 1/2^-$. There might exist configuration mixing in $\Xi(1690)$. The main component of $\Xi(1690)$ is $|70,^2 8, 1, 1, 1/2^{-}\rangle$, which slightly mixes with $|70,^2 10, 1, 1, 1/2^{-}\rangle$ and $|70,^4 8, 1, 1, 1/2^{-}\rangle$. Our predictions consist with the experimental observations. The recent mass calculations of a constituent quark model support the classification of $\Xi(1690)$ as a $J^P = \frac{1}{2}^-$ octet resonance [8]. The calculations of a Skyrme model [9] and unitary chiral approaches [12, 13] also indicated that $\Xi(1690)$ has $J^P = \frac{1}{2}^-$.

Since $\Xi(1690)$ corresponds to the physical state $|\Xi_{\frac{1}{2}}^{-}\rangle_2$ in Eq.(64), as the counterparts of $\Xi(1690)$, the other two physical states, $|\Xi_{\frac{1}{2}}^{-}\rangle_1 = -0.26|70,^2 8\rangle - 0.02|70,^4 8\rangle + 0.97|70,^2 10\rangle$ and $|\Xi_{\frac{1}{2}}^{-}\rangle_3 = 0.17|70,^2 8\rangle - 0.98|70,^4 8\rangle + 0.02|70,^2 10\rangle$, might be observed in experiments. It is easily seen that the main component of $|\Xi_{\frac{1}{2}}^{-}\rangle_1$ is $|70,^2 10, 1, 1, 1/2^{-}\rangle$ ($\sim 94\%$), while the $|\Xi_{\frac{1}{2}}^{-}\rangle_3$ is dominated by $|70,^4 8, 1, 1, 1/2^{-}\rangle$ ($\sim 96\%$). The strong decay properties of $|\Xi_{\frac{1}{2}}^{-}\rangle_1$ and $|\Xi_{\frac{1}{2}}^{-}\rangle_3$ were studied as well. The results were shown in Fig. 1. From the figure, we found that $|\Xi_{\frac{1}{2}}^{-}\rangle_1$ is a narrow state with a width of $\Gamma \sim 25$ MeV, while $|\Xi_{\frac{1}{2}}^{-}\rangle_3$ is a broad state with a width of ~ 100 MeV. The main decay channels of $|\Xi_{\frac{1}{2}}^{-}\rangle_1$ are $\Sigma \bar{K}$ and $\Lambda \bar{K}$, while the decays of $|\Xi_{\frac{1}{2}}^{-}\rangle_3$ is governed by $\Xi \pi$ and $\Lambda \bar{K}$.

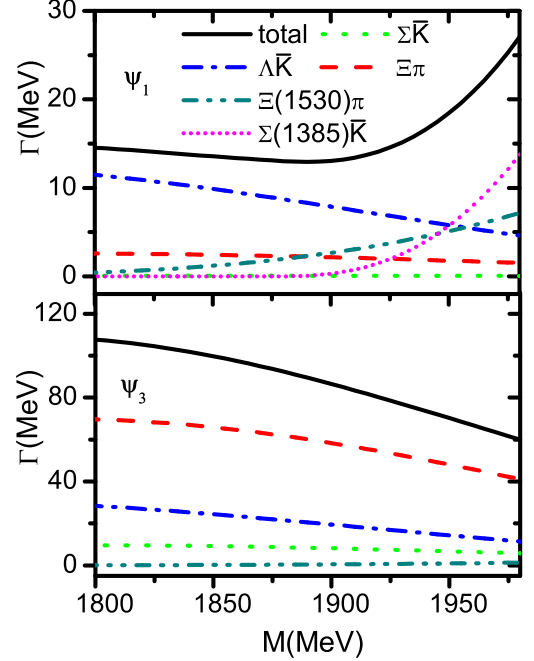


FIG. 1: The decay properties of the $|\Xi_{\frac{1}{2}}^{-}\rangle_1$ and $|\Xi_{\frac{1}{2}}^{-}\rangle_3$, respectively. Where $\Psi_1 \equiv |\Xi_{\frac{1}{2}}^{-}\rangle_1$ and $\Psi_3 \equiv |\Xi_{\frac{1}{2}}^{-}\rangle_3$.

C. $\Xi(1820)$

In 1987, Biagi *et al.* measured the spin-parity of $\Xi(1820)$ [18]. They found that its spin-parity is consistent with $J = 3/2^-$, which is in good agreement with the quark model predictions [2, 8, 10]. In the present work, the study of the well established resonance $\Xi(1820)$, on the one hand, can provide an important test of our model, on the other hand, can let us obtain more information about the nature of $\Xi(1820)$.

Assigning $\Xi(1820)$ to the negative states with $J^P = 1/2^-$, $3/2^-$ and $5/2^-$, respectively, their strong decays were calculated with our model. The results were listed in Tab. V, where we found that only the $|70,^2 8, 1, 1, \frac{3}{2}^-\rangle$ can be assigned to $\Xi(1820)$. The detail comparisons of theoretical predictions with measurements were shown in Tab. VII, from which it is seen that both the decay width and the partial decay ratios are in agreement with the measurements of ALITTI 69 [51]. Our predictions about the spin-parity values of $\Xi(1820)$ are consistent with the other model predictions and experimental determinations.

Although considering $\Xi(1820)$ as a pure state $|70,^2 8, 1, 1, \frac{3}{2}^-\rangle$ the theoretical predictions are in good agreement with the experimental observations, there still exists room for configuration mixing in $\Xi(1820)$ for the uncertainties of the experimental data. Chao *et al.* employed a quark model to study mass spectrum of Ξ resonances [2]. According to their study, $\Xi(1820)$ should be a mixed state, which dominates by the octet $|70,^2 8, 1, 1, \frac{3}{2}^-\rangle$ components ($\sim 90\%$),

TABLE V: The decay widths (MeV) of $\Xi(1820)^0$ with different assignments.

assignment	$\Xi\pi$	$\Sigma\bar{K}$	$\Lambda\bar{K}$	$\Xi(1530)\pi$	Γ_{total}
$ 70,^2 8, 1, 1, \frac{3}{2}^-\rangle$	2.85	10.63	7.25	11.98	32.71
$ 70,^4 8, 1, 1, \frac{1}{2}^-\rangle$	64.80	23.94	20.56	0.36	109.66
$ 70,^4 8, 1, 1, \frac{3}{2}^-\rangle$	4.56	0.26	0.72	11.95	17.49
$ 70,^4 8, 1, 1, \frac{5}{2}^-\rangle$	27.40	1.59	4.35	1.51	34.85
$ 70,^2 10, 1, 1, \frac{1}{2}^-\rangle$	4.05	5.98	5.14	1.43	16.60
$ 70,^2 10, 1, 1, \frac{3}{2}^-\rangle$	2.85	0.66	1.81	11.98	17.31

TABLE VI: The predicted total and partial decay width widths (MeV) and partial decay width ratios of $\Xi(1820)$ as the $|70,^2 8, 1, 1, \frac{3}{2}^-\rangle$ assignment compared with the experimental data of ALITTI 69 [51].

channel	Γ_i^{th}	Γ_{total}^{th}	Γ_{total}^{exp}	$\frac{\Gamma_i}{\Gamma_{total}} _{th}$	$\frac{\Gamma_i}{\Gamma_{total}} _{exp}$
$\Xi\pi$	2.9	32.8	24^{+15}_{-10}	0.09	0.1 ± 0.1
$\Sigma\bar{K}$	10.6			0.32	0.30 ± 0.15
$\Lambda\bar{K}$	7.3			0.22	0.30 ± 0.15
$\Xi(1530)\pi$	12.0			0.37	0.30 ± 0.15

while contains small components of $|70,^2 10, 1, 1, \frac{3}{2}^-\rangle$ ($\sim 9\%$) and $|70,^4 8, 1, 1, \frac{3}{2}^-\rangle$ ($\sim 1\%$). Thus, we considered the physical state $\Xi(1820)$ as an admixture between the octet and decuplet states with $J^P = \frac{3}{2}^-$. Using the CKM matrix method discussed in IV B, and fitting the observed strong decay properties, we obtained

$$\begin{pmatrix} |\Xi_{\frac{3}{2}^-}^1\rangle \\ |\Xi(1820)_{\frac{3}{2}^-}\rangle \\ |\Xi_{\frac{3}{2}^-}^3\rangle \end{pmatrix} = \begin{pmatrix} -0.08 & -0.98 & 0.17 \\ 0.96 & -0.13 & -0.26 \\ 0.27 & 0.14 & 0.95 \end{pmatrix} \begin{pmatrix} |70,^2 8\rangle \\ |70,^4 8\rangle \\ |70,^2 10\rangle \end{pmatrix}. \quad (65)$$

The theoretical results compared with the data were listed in Tab. VII, where we found that the predicted partial decay width ratios are in agreement with the experiment data of ALITTI 69 [51] as well. Considering configuration mixing effects in $\Xi(1820)$, the decay width is more close to the center values of observations. From the mixing parameters obtained in Eq. (65), it is seen that the main component of $\Xi(1820)$ is $|70,^2 8, 1, 1, \frac{3}{2}^-\rangle$, which is about 92%. As a mixed state, $\Xi(1820)$ also contains small components of $|70,^4 8, 1, 1, \frac{3}{2}^-\rangle$ ($\sim 0.02\%$) and $|70,^2 10, 1, 1, \frac{3}{2}^-\rangle$ ($\sim 0.07\%$). Our results are compatible with the predictions of Chao *et al.* [2]. It should be mentioned that $\Xi(1820)$ was also suggested to be a dynamically generated state with $J^P = 3/2^-$ [12, 13].

In brief, $\Xi(1820)$ could be approximately taken as a pure $|70,^2 8, 1, 1, \frac{3}{2}^-\rangle$ state. There maybe exist slightly configuration mixing in it. All the experimental observations of $\Xi(1820)$ could be well understood in the constituent quark model.

Considering $\Xi(1820)$ as a mixing state, its counterparts $|\Xi_{\frac{3}{2}^-}^1\rangle$ and $|\Xi_{\frac{3}{2}^-}^3\rangle$ in Eq. (65) might be observed in experiments as well. From Eq. (65) it is seen that the main components of $|\Xi_{\frac{3}{2}^-}^1\rangle$ and $|\Xi_{\frac{3}{2}^-}^3\rangle$ are $|70,^4 8, 1, 1, 3/2^-\rangle$ ($\sim 96\%$)

TABLE VII: The predicted total and partial decay width widths (MeV) and partial decay width ratios of $\Xi(1820)$ as the mixed state $|\Xi(1820)_{\frac{3}{2}^-}\rangle$ with mixing angles $\theta_{12} = 85^\circ$, $\theta_{13} = 170^\circ$ and $\theta_{23} = 165^\circ$. For a comparison, the experimental data of ALITTI 69 [51] are listed as well.

channel	Γ_i^{th}	Γ_{total}^{th}	Γ_{total}^{exp}	$\frac{\Gamma_i}{\Gamma_{total}} _{th}$	$\frac{\Gamma_i}{\Gamma_{total}} _{exp}$
$\Xi\pi$	2.1	23.3	24^{+15}_{-10}	0.09	0.1 ± 0.1
$\Sigma\bar{K}$	8.0			0.34	0.30 ± 0.15
$\Lambda\bar{K}$	9.2			0.40	0.30 ± 0.15
$\Xi(1530)\pi$	4.0			0.17	0.30 ± 0.15

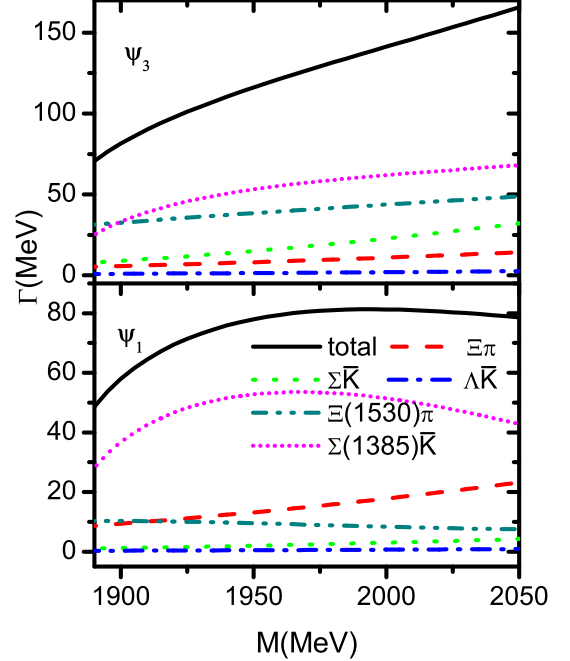


FIG. 2: The decay properties of the $|\Xi_{\frac{3}{2}^-}^1\rangle$ and $|\Xi_{\frac{3}{2}^-}^3\rangle$, respectively. Where $\Psi_1 \equiv |\Xi_{\frac{3}{2}^-}^1\rangle$ and $\Psi_3 \equiv |\Xi_{\frac{3}{2}^-}^3\rangle$.

and $|70,^2 10, 1, 1, 3/2^-\rangle$ ($\sim 90\%$), respectively. According to the quark model predictions [2], the masses of $|\Xi_{\frac{3}{2}^-}^1\rangle$ and $|\Xi_{\frac{3}{2}^-}^3\rangle$ are ~ 1910 MeV and ~ 1970 MeV, respectively. The strong decay properties of $|\Xi_{\frac{3}{2}^-}^1\rangle$ and $|\Xi_{\frac{3}{2}^-}^3\rangle$ were studied as well. The results were shown in Fig. 2. For the uncertainties of the mass predictions, we varied the masses of $|\Xi_{\frac{3}{2}^-}^1\rangle$ and $|\Xi_{\frac{3}{2}^-}^3\rangle$ from 1850 MeV to 2050 MeV. From the calculations, we found that if the masses of these two states are larger than the threshold of $\Sigma(1385)\bar{K}$, the decay channel $\Sigma(1385)\bar{K}$ dominates their decays. Furthermore, $\Xi(1530)\pi$ contributes significantly to the strong decays of these two states.

Finally, it should be pointed out that although the predicted masses of $|\Xi_{\frac{3}{2}^-}^1\rangle$ and $|\Xi_{\frac{3}{2}^-}^3\rangle$ are close to that of $\Xi(1950)$, the decay modes and partial decay width ratios are not consistent with the observations. Thus, $\Xi(1950)$ does not favor any $J^P = 3/2^-$ assignments.

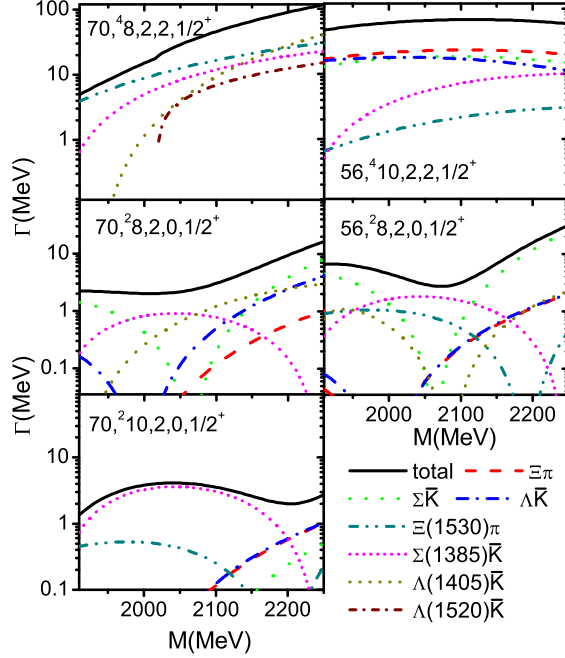
D. $\Xi(1950)$ 

FIG. 3: Strong decay properties of the $J^P = 1/2^+$ excitations in the $N = 2$ shell.

$\Xi(1950)$ was first observed by Badier *et al.* in the invariant mass distribution $\Xi\pi$ of $K^-p \rightarrow \Xi^-K\pi$ process [54], its observed mass and width are 1933 ± 16 MeV and $\Gamma \simeq 140 \pm 35$ MeV, respectively. Later, several experimental groups also found structures with a mass of $\sim 1950 \pm 50$ MeV in the other processes. $\Xi(1950)$ was only observed in $\Xi\pi$, $\Xi(1530)\pi$ and $\Lambda\bar{K}$ decay channels [1]. Most of these structures were observed in the $\Xi\pi$ channel. In the $\Lambda\bar{K}$ channel, only Biagi *et al.* claimed that they observed one narrow structure ($\Gamma \simeq 25 \pm 15$ MeV) with a mass of $M \simeq 1963$ MeV [18]. They estimated an upper limit on the ratio of partial widths $\Gamma(\Sigma\bar{K})/\Gamma(\Lambda\bar{K})$ of 2.3, and also suggested that the spin-parity of this resonance should be $5/2^+$ or its spin should be greater than $5/2$ in the natural spin-parity series $7/2^-, 9/2^+, \text{etc.}$ While in the $\Xi(1530)\pi$ channel, only Briefel *et al.* reported that they observed a broad structure ($\Gamma \simeq 60 \pm 39$ MeV) with a mass of $M \simeq 1964$ MeV [55]. Although $\Xi(1950)$ is a three-star Ξ resonance listed in PDG, not much can be said about its properties.

1. $J^P = 5/2^-$ assignment

$\Xi(1950)$ was first classified as the pure octet Ξ resonance with $J^P = 5/2^-$ by Alitti *et al.* [17]. In 1968, they observed a Ξ resonance whose mass and width are $M = 1930 \pm 20$

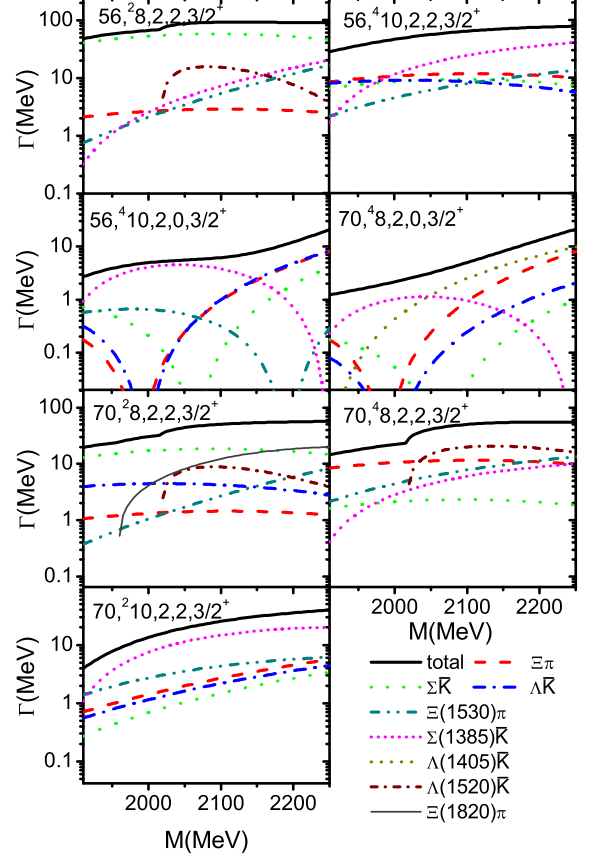


FIG. 4: Strong decay properties of the $J^P = 3/2^+$ excitations in the $N = 2$ shell.

MeV and $\Gamma = 80 \pm 40$ MeV, respectively. The resonance parameters were very close to the observations of Badier *et al.* in 1965 [54]. The Gell-Mann-Okubo mass formula indicates this state might be the pure octet Ξ resonance with $J^P = 5/2^-$ [21, 56]. The detailed SU(3) study of the total and partial decay widths of the $J^P = 5/2^-$ octet baryons seemed to give a reasonable and consistent picture [17]. This classification was also supported by some studies of the mass spectrum of Ξ resonances in various quark models [2, 8].

$\Xi(1950)$ as an assignment to the $J^P = 5/2^-$ octet Ξ resonance, we studied its strong decay properties, the results were listed in Tab. VIII. It is seen that the $J^P = 5/2^-$ assignment is a broad state with a width of ~ 100 MeV. Its strong decays are dominated by the $\Xi\pi$ channel. The partial decay widths of $\Xi(1530)\pi$ and $\Lambda\bar{K}$ are sizeable. Our predictions are in compatible with those in [17]. Thus, the broad Ξ resonances observed in $\Xi\pi$ channel might be good candidates for the $J^P = 5/2^-$ octet state.

As a by-product, we calculated the strong decays of the other members of $J^P = 5/2^-$ octet baryons, $N(1675)\frac{5}{2}^-$, $\Sigma(1775)\frac{5}{2}^-$ and $\Lambda(1830)\frac{5}{2}^-$. The results were listed in Tab. VIII as well. From the table, it is found that our predic-

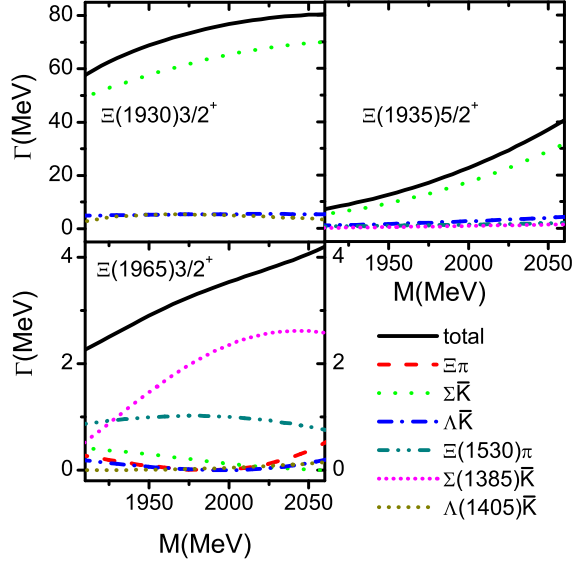


FIG. 5: Strong decay properties of $J^P = 3/2^+$ and $J^P = 5/2^+$ mixed states suggested by Chao *et al.*[2].

TABLE VIII: The total and partial decay widths (MeV) of the well-established with four stars baryons $N(1675)$, $\Sigma(1775)$ and $\Lambda(1830)$, which correspond to $|70, 4/2, 1, 1, \frac{5}{2}^-\rangle$. The data are obtained from PDG.

assignment	channel	Γ_i^{th}	Γ_{total}^{th}	Γ_{total}^{exp}	$\frac{\Gamma_i}{\Gamma_{total}} _{th}$	$\frac{\Gamma_i}{\Gamma_{total}} _{exp}$
$N(1675)\frac{5}{2}^-$	$n\pi$	25.3	81	130 ~ 165	0.31	0.35–0.45
	$\Delta\pi$	50.6			0.62	0.50–0.60
	$N\eta$	5.8			0.07	0.01
$\Sigma(1775)\frac{5}{2}^-$	$\Sigma\pi$	8.0	76	105 ~ 135	0.11	0.02–0.05
	$\Lambda\pi^0$	19.1			0.25	0.14–0.20
	$n\bar{K}$	32.1			0.42	0.37–0.43
	$\Sigma(1385)\pi$	4.8			0.06	0.08–0.12
	$\Delta(1232)\bar{K}$	1.0			0.01	...
	$\Lambda(1520)\pi$	11.2			0.14	0.17–0.23
$\Lambda(1830)\frac{5}{2}^-$	$\Sigma\pi$	52.2	94	60 ~ 110	0.55	0.35–0.75
	$\Sigma(1385)\pi$	41.7			0.45	> 0.15
$\Xi(1950)\frac{5}{2}^-$	$\Xi\pi$	71.33	105	80 ± 40	0.68	...
	$\Sigma\bar{K}$	7.8			0.07	...
	$\Lambda\bar{K}$	13.6			0.13	...
	$\Xi(1530)\pi$	10.9			0.10	...
	$\Sigma(1385)\bar{K}$	1.2			0.01	...

tions of the strong decay properties of $N(1675)\frac{5}{2}^-$, $\Sigma(1775)\frac{5}{2}^-$ and $\Lambda(1830)\frac{5}{2}^-$ are in reasonable agreement with the observations.

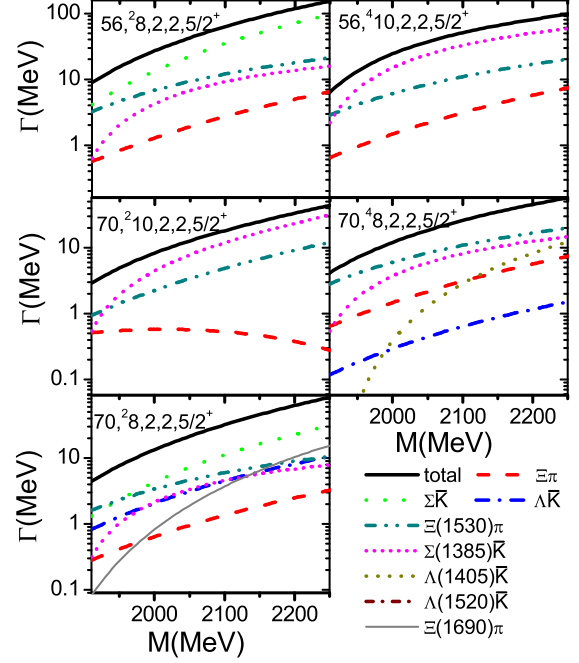


FIG. 6: Strong decay properties of the $J^P = 5/2^+$ excitations in the $N = 2$ shell.

2. $J^P = 1/2^-$ assignment

Recently, Valderrama, Xie and Nieves proposed the existence of a spin-parity state $J^P = 1/2^-$ decuplet belonging to $\Xi(1950)$ [19]. Now we discuss the possibilities of $\Xi(1950)$ as an assignment to the $J^P = 1/2^-$ states. In Sec. IV B, we predicted $\Xi(1690)$ is a mixed state with $J^P = 1/2^-$. According to the mass calculations of constituent quark models [2, 11], the masses of the counterparts of $\Xi(1690)$, $|\Xi\frac{1}{2}^-\rangle_1$ and $|\Xi\frac{1}{2}^-\rangle_3$, might be close to 1950 MeV. Thus, they might be candidates for $\Xi(1950)$. The strong decay properties of $|\Xi\frac{1}{2}^-\rangle_1$ and $|\Xi\frac{1}{2}^-\rangle_3$ had been studied in Sec. IV B (see Fig. 1). Considering $|\Xi\frac{1}{2}^-\rangle_1$ as an assignment to $\Xi(1950)$, both the decay width and partial width ratio,

$$\Gamma \simeq 27 \text{ MeV}, \frac{\Gamma(\Sigma\bar{K})}{\Gamma(\Lambda\bar{K})} \simeq 2.0, \quad (66)$$

are in agreement with the observations of Biagi 87C [18], however, the spin-parity $J^P = 1/2^-$ disagrees with their suggestion. While assigning $|\Xi\frac{1}{2}^-\rangle_3$ to $\Xi(1950)$, its width and partial width ratios

$$\Gamma \simeq 84 \text{ MeV}, \frac{\Gamma(\Sigma\bar{K})}{\Gamma(\Lambda\bar{K})} \simeq 1.6, \frac{\Gamma(\Xi\pi)}{\Gamma(\Sigma\bar{K})} \simeq 2.3, \quad (67)$$

are consistent with those of the broad structures observed in $\Xi\pi$ channel. Thus, the spin-parity $1/2^-$ mixed state $|\Xi\frac{1}{2}^-\rangle_3$ could be a good assignment to $\Xi(1950)$.

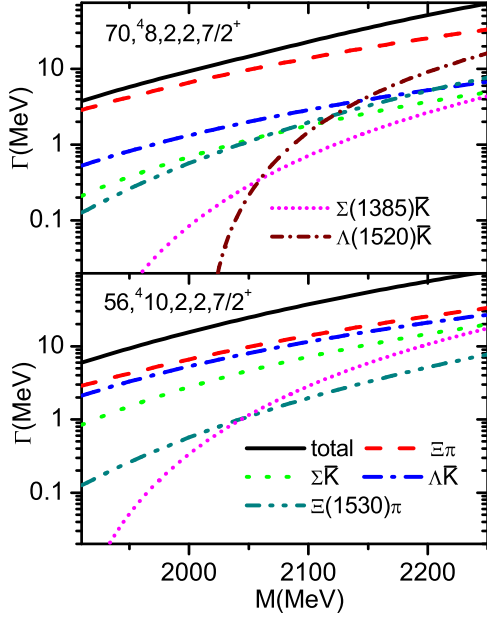


FIG. 7: Strong decay properties of the $J^P = 7/2^+$ excitations in the $N = 2$ shell.

3. $J^P = 1/2^+$ assignment

In Ref. [9], Oh predicted that $\Xi(1950)$ might have $J^P = 1/2^+$ in the Skyrme model. We calculated the strong decays of all the excitations of Ξ with $J^P = 1/2^+$ in the $N = 2$ shell. The results were shown in Fig. 3. From the figure, it is found that if the second orbital excitation $[56, ^4_{10}, 2, 2, \frac{1}{2}^+]$ is considered as an assignment to $\Xi(1950)$, the decay width and partial width ratios are

$$\Gamma \simeq 53 \text{ MeV}, \frac{\Gamma(\Sigma\bar{K})}{\Gamma(\Lambda\bar{K})} \simeq 0.88, \frac{\Gamma(\Xi\pi)}{\Gamma(\Sigma\bar{K})} \simeq 1.27. \quad (68)$$

The decay width and decay modes are consistent with the observations of Goldwasser *et al.* [57]. It should be pointed out that the predicted mass of quark model for $[56, ^4_{10}, 2, 2, \frac{1}{2}^+]$ is $\sim 2 \text{ GeV}$, which is slightly larger than the observation.

4. $J^P = 3/2^+$ assignment

Furthermore, we calculated the strong decays of all the excitations of Ξ with $J^P = 3/2^+$ in the $N = 2$ shell. The results were shown in Fig. 4. It is found that the second orbital excitation $[56, ^4_{10}, 2, 2, \frac{3}{2}^+]$ might be a candidate for $\Xi(1950)$. The decay width

$$\Gamma \simeq 36 \text{ MeV}, \quad (69)$$

and the partial width ratios

$$\frac{\Gamma(\Sigma\bar{K})}{\Gamma(\Lambda\bar{K})} \simeq 0.88, \frac{\Gamma(\Xi\pi)}{\Gamma(\Sigma\bar{K})} \simeq 1.27, \frac{\Gamma(\Xi\pi)}{\Gamma(\Xi(1530)\pi)} \simeq 3.16 \quad (70)$$

are in agreement with the observations of Biagi 87C [18] and APSELL 70 [53]. However, the spin-parity of $[56, ^4_{10}, 2, 2, \frac{3}{2}^+]$ do not consist with the moment analysis of Biagi 87C [18].

Including configuration mixing effects, Chao *et al.* predicted two $J^P = 3/2^+$ mixed states with masses of $M = 1930$ and 1965 MeV , respectively [2]. With their mixing scheme, we predicted the strong decays of the two states. The results were shown in Fig. 5. It is obviously seen that the decay properties of these mixed states are not in agreement with any observations of $\Xi(1950)$.

TABLE IX: The total and partial decay widths (MeV) of the well-established four-star baryons $N(1680)$, $\Sigma(1915)$ and $\Lambda(1820)$, which are considered the pure $[56, ^2_8, 2, 2, \frac{5}{2}^+]$ state. The data are obtained from PDG.

assignment	channel	Γ_i^{th}	Γ_{total}^{th}	Γ_{total}^{exp}	$\frac{\Gamma_i}{\Gamma_{total}} _{th}$	$\frac{\Gamma_i}{\Gamma_{total}} _{exp}$
$N(1680)\frac{5}{2}^+$	$n\pi$	38.0	59	120 ~ 140	0.64	0.65–0.70
	$\Delta\pi$	21.0			0.36	...
	$N\eta$	0.4			0.01	0.0–0.01
	ΛK	0.03			0	...
$\Sigma(1915)\frac{5}{2}^+$	$N\bar{K}$	1.2	63	80 ~ 160	0.02	0.05–0.15
	$\Lambda\pi$	10.4			0.16	...
	$\Sigma\pi$	26.7			0.42	...
	$\Sigma(1385)\pi$	6.2			0.10	...
	$\Delta(1232)\bar{K}$	18.4			0.29	...
$\Lambda(1820)\frac{5}{2}^+$	$N\bar{K}$	14.8	30	70 ~ 90	0.49	0.55–0.65
	$\Sigma\pi$	5.8			0.19	0.08–0.14
	$\Sigma(1385)\pi$	9.8			0.32	...
$\Xi(1963)\frac{5}{2}^+$	$\Xi\pi$	1.0	19	25 ± 15	0.05	
	$\Sigma\bar{K}$	9.2			0.48	
	$\Lambda\bar{K}$	0.8			0.04	
	$\Xi(1530)\pi$	5.2			0.27	
	$\Sigma(1385)\bar{K}$	2.5			0.13	

5. $J^P = 5/2^+$ assignment

Recently, Valderrama, Valderrama Xie and Nieves [19] predicted that the narrow structure with a mass of $M \simeq 1963 \text{ MeV}$ observed in the $\Lambda\bar{K}$ channel by Biagi *et al.* [18] (denoted by $\Xi(1963)$) could be assigned to the partner of the $J^P = 5/2^+$ $N(1680)$, $\Lambda(1820)$ and $\Sigma(1915)$ resonances. According to the classification of quark model, these resonances could be roughly considered as the $[56, ^2_8, 2, 2, \frac{5}{2}^+]$ configuration [58]. Firstly, we calculated the strong decays of the $N(1680)$, $\Lambda(1820)$ and $\Sigma(1915)$ states, which were listed in Tab. IX. From the table, it is found that the decay properties of $N(1680)$, $\Lambda(1820)$ and $\Sigma(1915)$ could be roughly understood by taking them as the $[56, ^2_8, 2, 2, \frac{5}{2}^+]$ configuration.

Assigning $\Xi(1963)$ to the $[56,^2 8, 2, 2, \frac{5}{2}^+]$ configuration, the predicted strong decay properties were shown in Tab. IX as well. It is seen that although the decay width is in agreement with the data, the partial decay width ratios are not consistent with the observations of Biagi *et al.* [18] at all.

Furthermore, Chao *et al.* also predicted a mixed states with $J^P = 5/2^+$ having a mass of $M = 1935$ MeV [2]. With their mixing scheme, its strong decays were studied. The results were shown in Fig. 5 as well. It is seen that the strong decays are dominated by the $\Sigma\bar{K}$ channel, which disagree with any

observations of $\Xi(1950)$.

In brief, there might be several Ξ resonances in the 1900 – 2000 MeV region observed in experiments. These states are most likely to correspond to the pure octet Ξ resonance with $J^P = 5/2^-$, the mixed state $|\Xi\frac{1}{2}^-\rangle_3$ with $J^P = 1/2^-$ (its main component is $|70,^4 8, 1, 1, \frac{1}{2}^-\rangle$), the second orbital excitation $[56,^4 10, 2, 2, \frac{1}{2}^+]$ with $J^P = 1/2^+$, etc. These states can be easily distinguished by the measurements of their partial decay width ratios, $\Gamma(\Lambda\bar{K})/\Gamma(\Sigma\bar{K})$ and $\Gamma(\Sigma\bar{K})/\Gamma(\Xi\pi)$.

TABLE X: The decay widths (MeV) of $\Xi(2030)$ with different assignments.

assignment	$\Xi\pi$	$\Sigma\bar{K}$	$\Lambda\bar{K}$	$\Xi(1530)\pi$	$\Sigma(1385)\bar{K}$	$\Lambda(1405)\bar{K}$	$\Lambda(1520)\bar{K}$	Γ_{total}	$\Gamma(\Lambda\bar{K}) : \Gamma(\Sigma\bar{K})$
$[56,^2 8, 2, 2, \frac{5}{2}^+]$	1.6	18.5	1.3	8.2	5.7	0.4	0.01	35.8	0.07
$[70,^2 8, 2, 2, \frac{3}{2}^+]$	1.4	17.9	4.5	1.4	0.6	1.5	5.4	32.7	0.25
$[70,^2 8, 2, 2, \frac{5}{2}^+]$	0.8	5.8	2.7	4.1	2.8	0.05	0.07	16.3	0.46

E. $\Xi(2030)$

$\Xi(2030)$ is a three-star state listed in PDG. It mainly decays into $\Sigma\bar{K}$ and $\Lambda\bar{K}$ channels. The decay ratios into the other channels, such as $\Xi\pi$ and $\Xi(1530)\pi$, are small. The measured decay width and partial decay width ratio are

$$\Gamma \simeq 21 \pm 6 \text{ MeV}, \quad \frac{\Gamma(\Lambda\bar{K})}{\Gamma(\Sigma\bar{K})} \simeq 0.22 \pm 0.09. \quad (71)$$

A moment analysis of the HEMINGWAY 77 data indicated at a level of three standard deviations that $J \geq 5/2$ [20].

We analyzed the strong decay properties for all the configurations in the $N = 2$ shell, which were shown in Figs. 3-7. From the figures, we found that only three excitations $[56,^2 8, 2, 2, \frac{5}{2}^+]$, $[70,^2 8, 2, 2, \frac{3}{2}^+]$ and $[70,^2 8, 2, 2, \frac{5}{2}^+]$ have comparable decay widths with that of $\Xi(2030)$, and mainly decay into $\Sigma\bar{K}$ channel. Considering them as assignments to $\Xi(2030)$, we collected their decay properties in Tab. X, where we found that both the decay width and the partial decay ratio

$$\Gamma \simeq 33 \text{ MeV}, \quad \frac{\Gamma(\Lambda\bar{K})}{\Gamma(\Sigma\bar{K})} \simeq 0.25. \quad (72)$$

of the $[70,^2 8, 2, 2, \frac{3}{2}^+]$ configuration are in good agreement with the observations. However, its spin $J = 3/2$ disagrees with the moment analysis of the HEMINGWAY 77 data [20].

As a whole, if we do not care about the moment analysis of the HEMINGWAY 77 data [20], $\Xi(2030)$ favors the $[70,^2 8, 2, 2, \frac{3}{2}^+]$ assignment. $\Xi(2030)$ could not be assigned to any pure $J^P = 7/2^+$ states or any admixtures between them. If the spin-parity of $\Xi(2030)$ is $J^P = 5/2^+$, it is most likely to be a mixed state, for no pure $J^P = 5/2^+$ configuration could explain the data.

V. SUMMARY

In this work, we studied the strong decays of the Ξ baryons within $N \leq 2$ shells in a chiral quark model. The strong decay properties of these well-established ground decuplet baryons could be reasonably described. We found that $\Xi(1690)$ should be assigned to the spin-parity $J^P = 1/2^-$ state $[70,^2 8, 1, 1, \frac{1}{2}^-]$, which might slightly mix with the other configurations. The strong decays of the physical partners of $\Xi(1690)$, $|\Xi\frac{1}{2}^-\rangle_1$ and $|\Xi\frac{1}{2}^-\rangle_3$ were analyzed as well. $|\Xi\frac{1}{2}^-\rangle_1$ might be observed in the $\Sigma\bar{K}$ and $\Lambda\bar{K}$ channels, while $|\Xi\frac{1}{2}^-\rangle_3$ is possibly observed in the $\Xi\pi$ and $\Lambda\bar{K}$ channels.

The strong decay properties of $\Xi(1820)$ could be well understood by assigning it to the $[70,^2 8, 1, 1, \frac{3}{2}^-]$. There might exist slight configuration mixing in $\Xi(1820)$. Its main component is $[70,^2 8, 1, 1, \frac{3}{2}^-]$ ($\sim 92\%$). Considering the configuration mixing effects, we also studied the strong decay properties of the physical partners of $\Xi(1820)$, $|\Xi\frac{3}{2}^-\rangle_1$ and $|\Xi\frac{3}{2}^-\rangle_3$. The observations in the $\Sigma(1385)\bar{K}$ and $\Xi(1530)\pi$ channels are crucial to look for the other $J^P = 3/2^-$ states $|\Xi\frac{3}{2}^-\rangle_1$ and $|\Xi\frac{3}{2}^-\rangle_3$ in future experiments.

The situation for $\Xi(1950)$ is very complicated. Several Ξ resonances in the 1900 – 2000 MeV region might have been observed in experiments. The broad Ξ resonances observed in $\Xi\pi$ channel might be good candidates for the $J^P = 5/2^-$ octet state or the mixed state $|\Xi\frac{1}{2}^-\rangle_3$ with $J^P = 1/2^-$. The Ξ resonance with moderate width observed by Goldwasser *et al.* [57] might correspond to the $J^P = 1/2^+$ excitation $[56,^4 10, 2, 2, \frac{1}{2}^+]$. The second orbital excitation $[56,^4 10, 2, 2, \frac{3}{2}^+]$ and the mixed state $|\Xi\frac{1}{2}^-\rangle_1$ might be candidates for narrow width state observed in the $\Lambda\bar{K}$ channel, however, their spin-parity is not consistent with a moment analy-

sis of the data. The partial decay ratios, $\Gamma(\Lambda\bar{K})/\Gamma(\Sigma\bar{K})$ and $\Gamma(\Sigma\bar{K})/\Gamma(\Xi\pi)$, are sensitive to different assignments. Thus, the measurements of these ratios are crucial to uncover many puzzles in $\Xi(1950)$.

In present work, $\Xi(2030)$ as any spin-parity $J^P = 7/2^+$ states should be excluded. The observations of $\Xi(2030)$ do not favor any pure $J^P = 5/2^+$ configuration as well. If we do not care about the moment analysis of the HEMINGWAY 77 data, $\Xi(2030)$ favors the $|70, 2, 8, 2, 2, \frac{3}{2}^+\rangle$ assignment. Further observations in the $\Xi(1530)\pi$ and $\Sigma(1385)\bar{K}$ channels are necessary.

To provide helpful information for the search for the missing Ξ baryons, in Figs. 3-7 our predictions of their strong decay properties were shown as well. From our theoretical results, we found that the strong decays of many Ξ resonances

are dominated by the $\Xi(1530)\pi$ and $\Sigma(1385)\bar{K}$, thus, in these decay channels, we might find some new Ξ resonances as well.

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